

# ECE 330: Power Circuits and Electromechanics

Lecture 26

2019-12-06

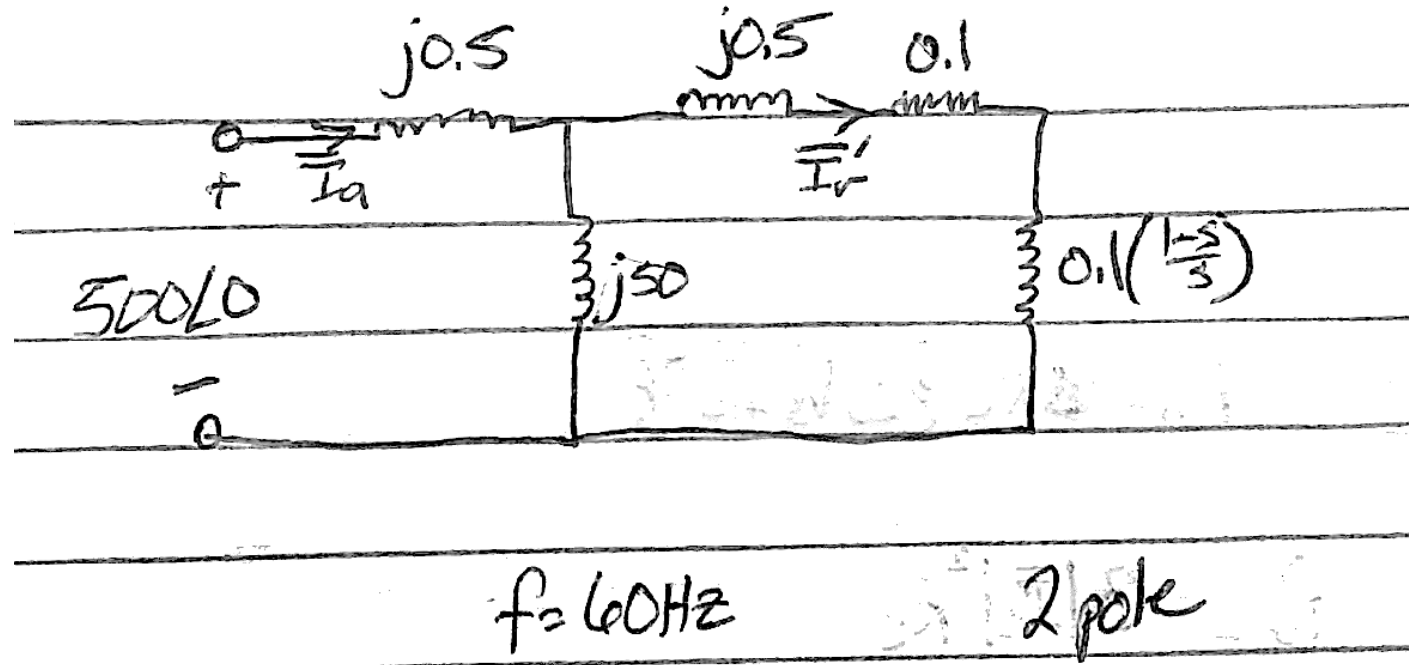
# Last Time

- Induction Machines
- Equivalent Circuit

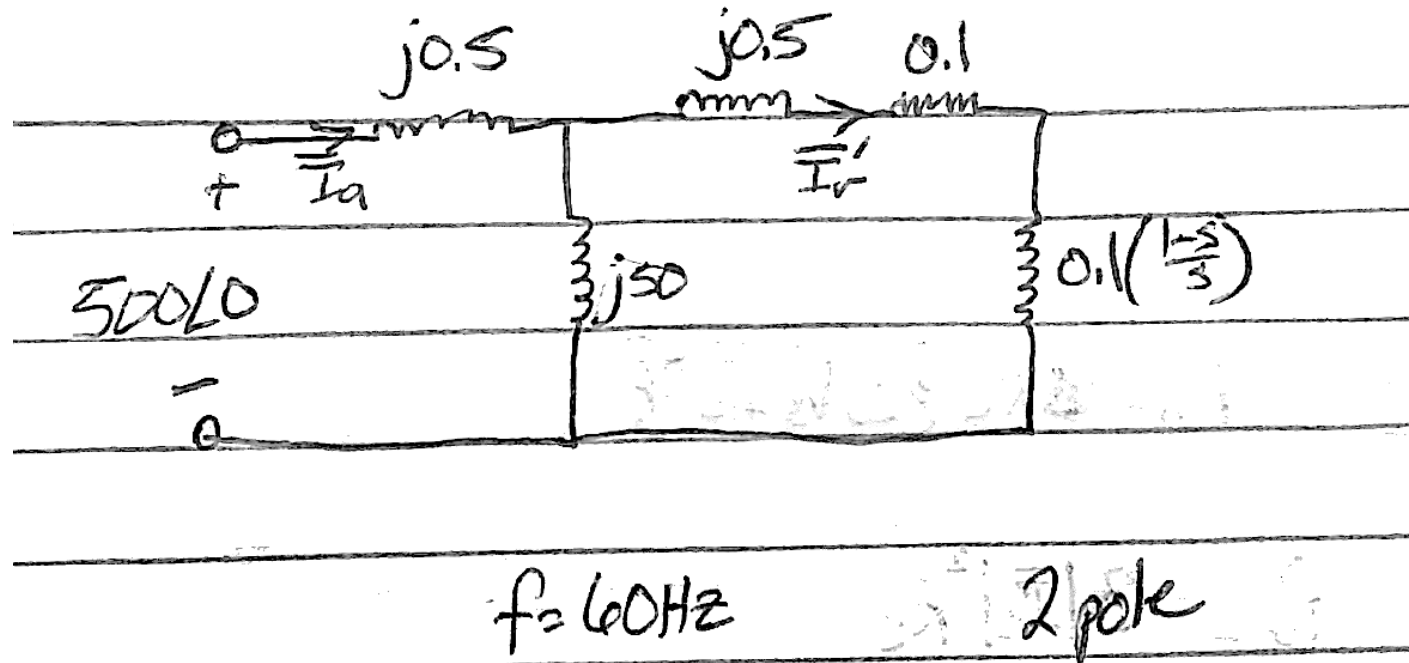
# Today

- Torque vs. Slip
- Examples

# Example: Torque vs. Slip



# Example: Torque vs. Slip



The torque will vary with  $s$

$$T^e = \frac{P_{ag}}{\omega_s \left(\frac{2}{p}\right)}$$

$$P_{ag} = 3|\bar{I}_r'|^2 \left(\frac{R_r'}{s}\right)$$

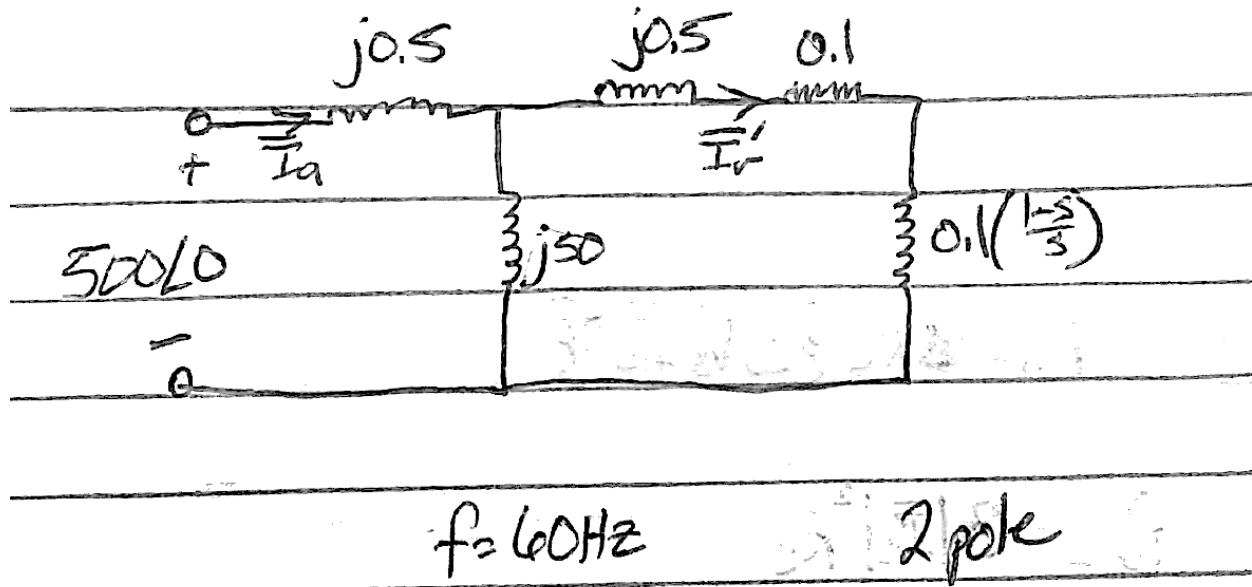
$$\bar{I}_r' = \bar{I}_a - \bar{I}_m$$

$$\bar{I}_m = \frac{\bar{V}_{an} - j0.5\bar{I}_a}{j50}$$

$$\bar{I}_a = \frac{\bar{V}_{an}}{Z_{tot}}$$

$$\bar{Z}_{tot} = j0.5 + \left( \frac{1}{j50} + \frac{1}{\frac{0.1}{s} + j0.5} \right)^{-1}$$

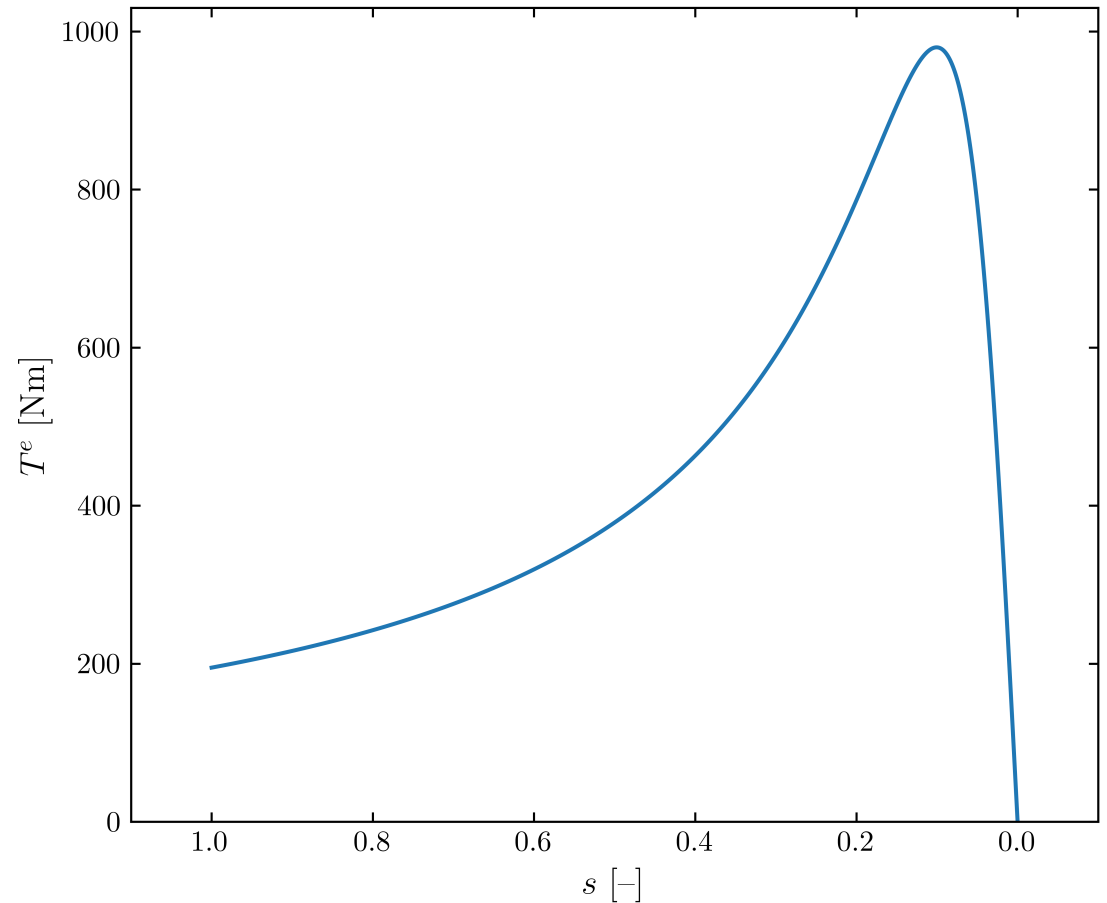
# Example: Torque vs. Slip



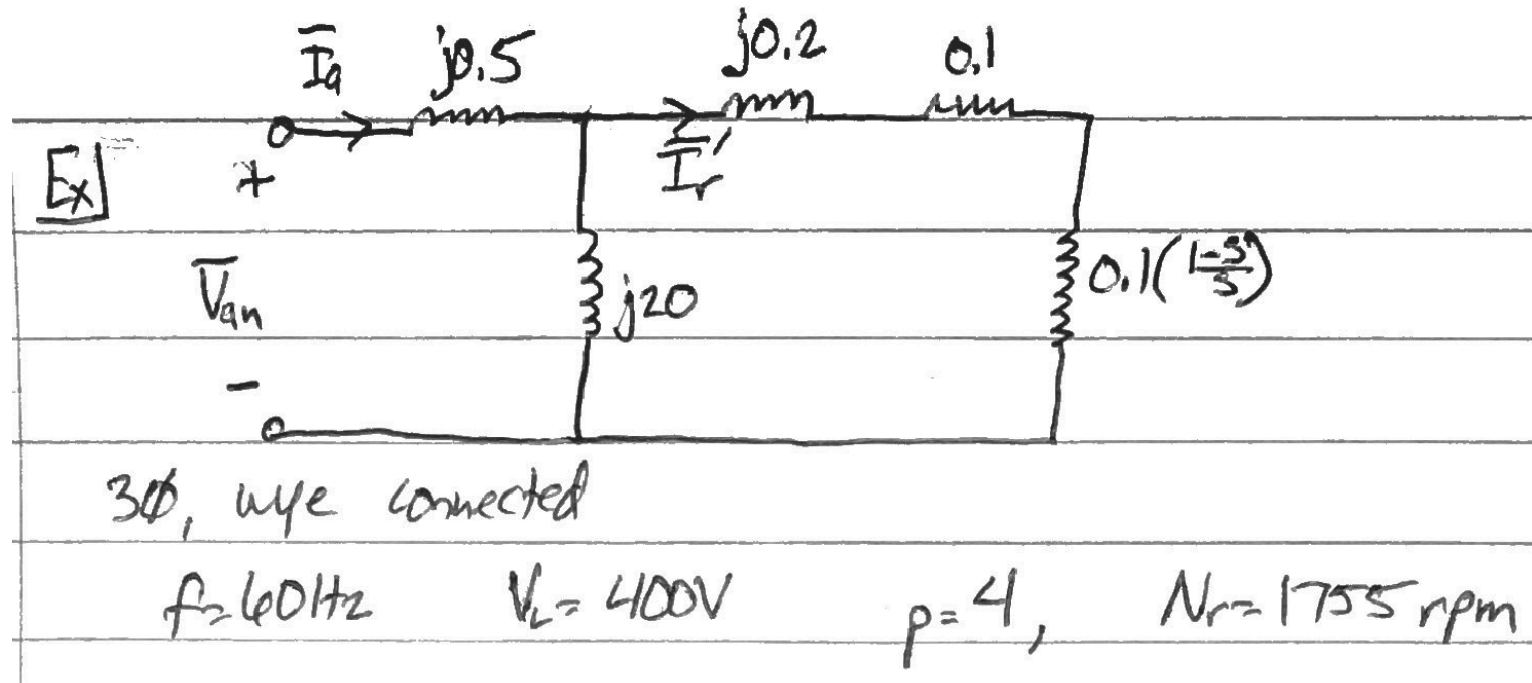
When  $s=0$ ,  $T^e = 0$

Maximum is  $T^e$

Decays with increase  $s$  after reaching max



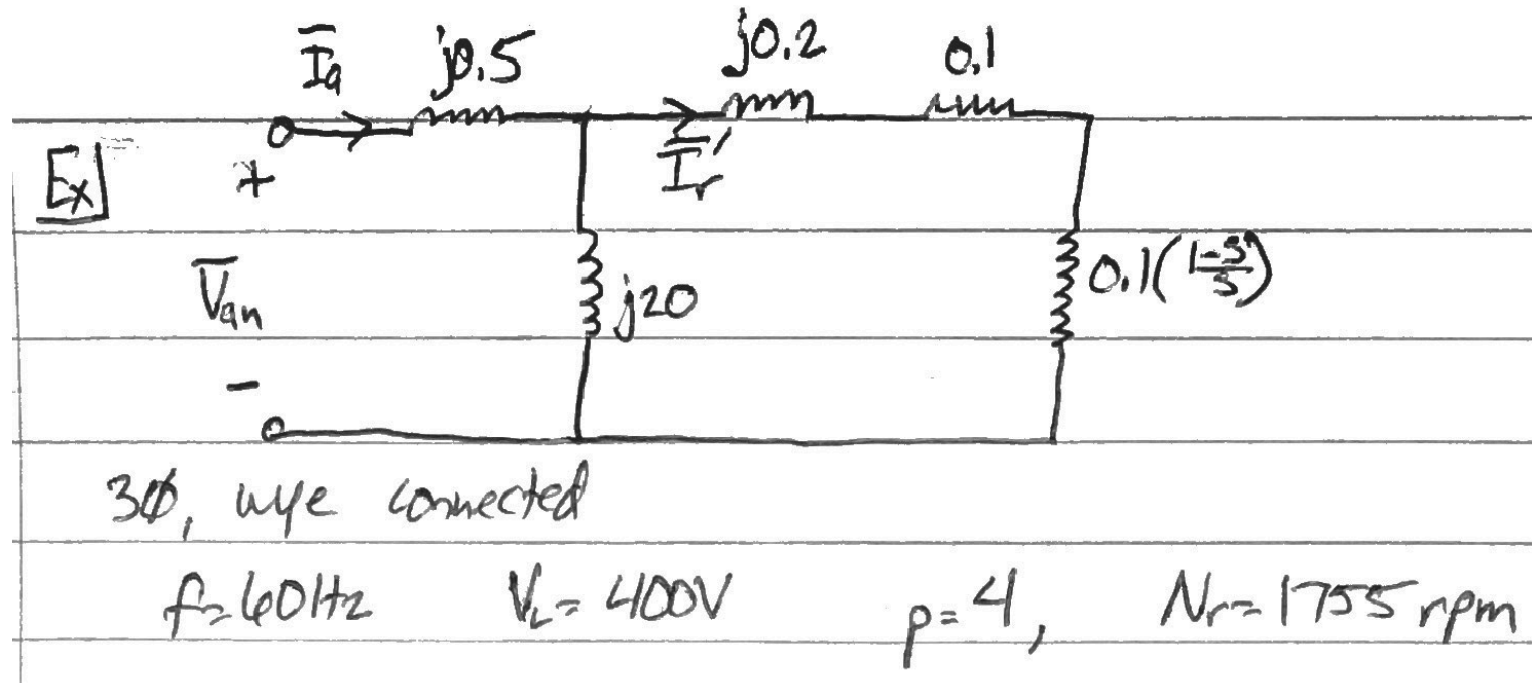
# Example



What is the torque?

- a) 98.09 Nm
- b) 1232.6 Nm
- c) 196.18 Nm
- d) 21.07 Nm

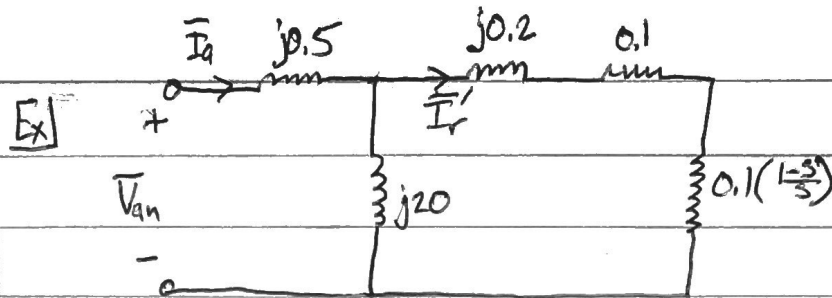
# Example



What is the torque?

- a) 98.09 Nm
- b) 1232.6 Nm
- c) 196.18 Nm
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3 $\phi$ , wye connected

$$f = 60 \text{ Hz}$$

$$V_L = 400 \text{ V}$$

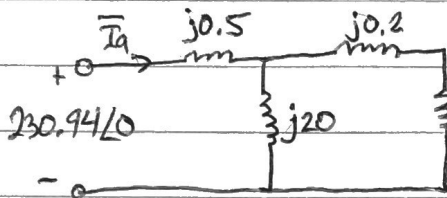
$$p = 4$$

$$N_r = 1755 \text{ rpm}$$

Find:  $T_e$

Solution:  $N_s = \left(\frac{2}{p}\right) 2\pi(60) \Rightarrow N_s = 1800 \text{ rpm}$

$$s = \frac{N_s - N_r}{N_s} \Rightarrow s = \frac{1800 - 1755}{1800} \Rightarrow \boxed{s = 0.025}$$



$$\bar{I}_a = \frac{V_{an}}{Z_{eq}} \Rightarrow \bar{I}_a = \frac{230.94/0}{4.041/20.958^\circ}$$

$$\boxed{\bar{I}_a = 57.149 \angle -20.958^\circ}$$

$$\bar{I}_r' = \frac{230.94/0 - j0.5\bar{I}_a}{4 + j0.2} \Rightarrow \text{[Scribbled out calculation]}$$

$$\bar{I}_r' = \frac{222.237 \angle -6.893^\circ}{4 + j0.2} \Rightarrow \bar{I}_r' = 55.512 \angle -9.756^\circ$$

$$P_{AG} = 3(55.512)^2(4) \Rightarrow P_{AG} = 36.978 \text{ kW}$$

$$T_e = \frac{P_{AG}}{\frac{2}{p}\omega_s} \Rightarrow T_e = \frac{36.978 \text{ kW}}{\left(\frac{2}{4}\right)(2\pi(60))} \Rightarrow \boxed{T_e = 196.18 \text{ Nm}}$$

# What does “starting” mean?

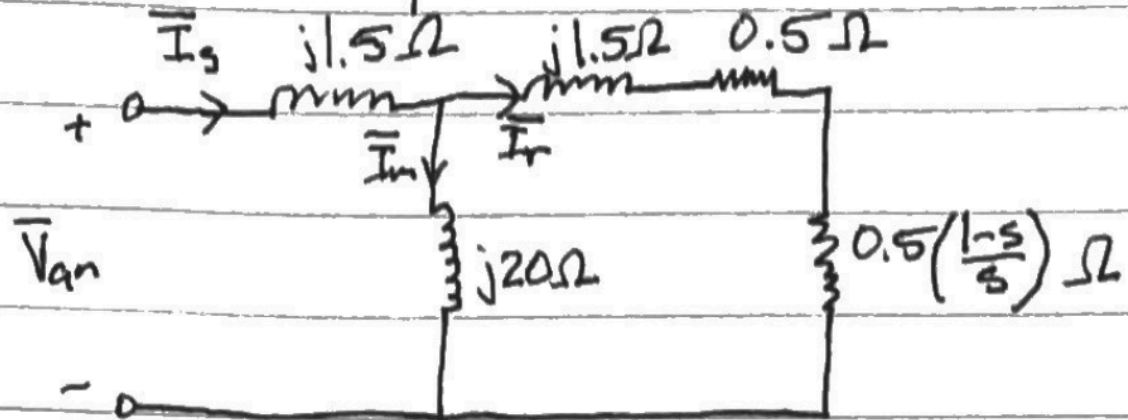
- Calculate torque at motor starting
- At starting, motor is just about to move, but hasn't started moving yet  
 $\omega_m = 0, s = 1$
- The  $R'_r \left( \frac{1-s}{s} \right)$  term in circuit becomes a short
- Evaluate the circuit as usual to find the torque

# Example

Fall 2003 Final

7) 3  $\phi$ , 6-pole, 60Hz, 440V

$\omega_m = 1120$  rpm



What is the current drawn by the system at start?

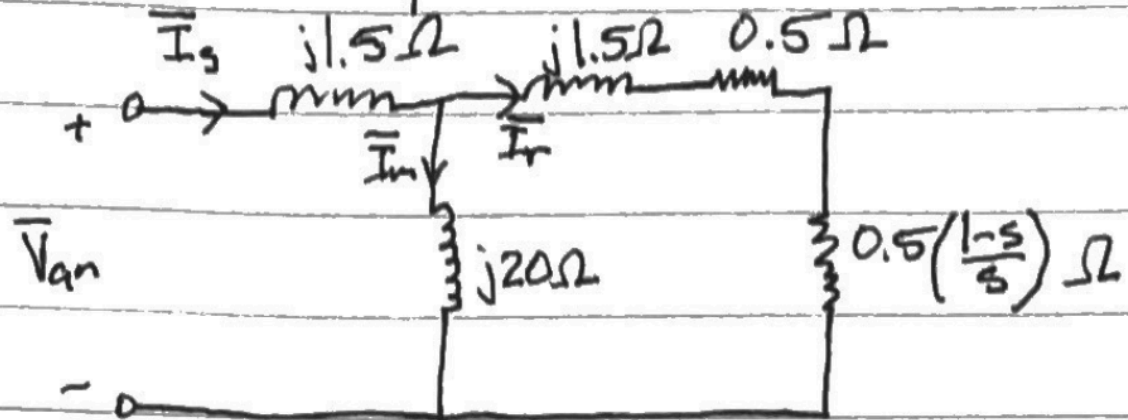
- a)  $149.81 \angle -81.54^\circ$  A
- b)  $86.49 \angle -81.54^\circ$  A
- c)  $11.82 \angle -90^\circ$  A
- d)  $100 \angle -81.54^\circ$  A

# Example

Fall 2003 Final

7) 3  $\phi$ , 6-pole, 60Hz, 440V

$\omega_m = 1120$  rpm



What is the current drawn by the system at start?

a)  $149.81\angle -81.54^\circ$  A

**b)  $86.49\angle -81.54^\circ$  A**

c)  $11.82\angle -90^\circ$  A

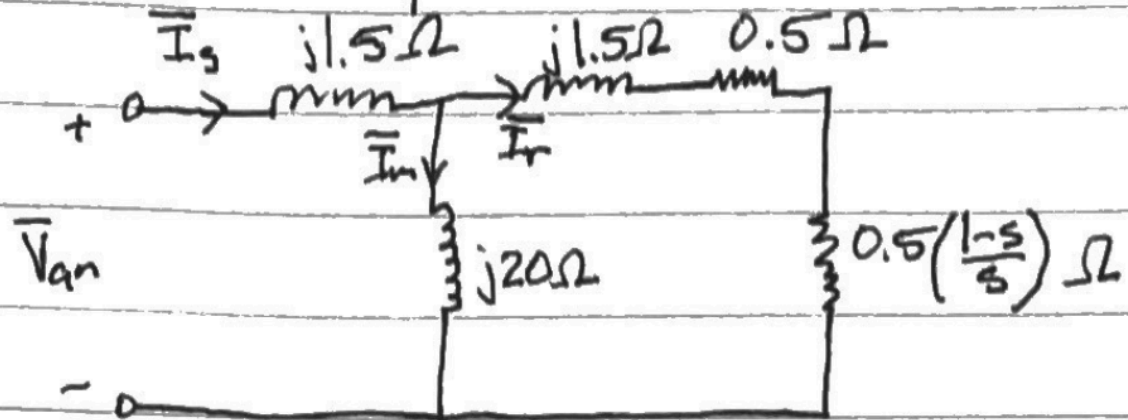
d)  $100\angle -81.54^\circ$  A

# Example

Fall 2003 Final

7) 3  $\phi$ , 6-pole, 60Hz, 440V

$\omega_m = 1120$  rpm



What is the starting torque?

a) 29.76 Nm

b) 9.92 Nm

c) 187.0 Nm

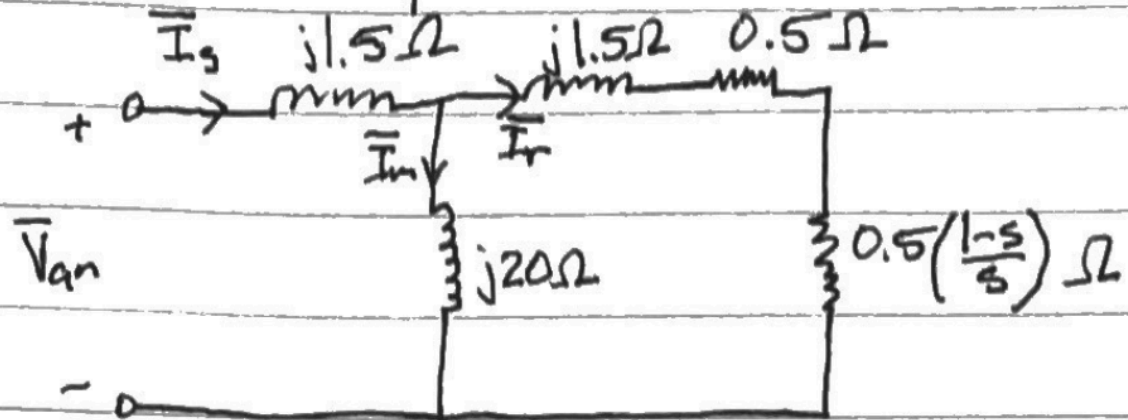
d) 89.3 Nm

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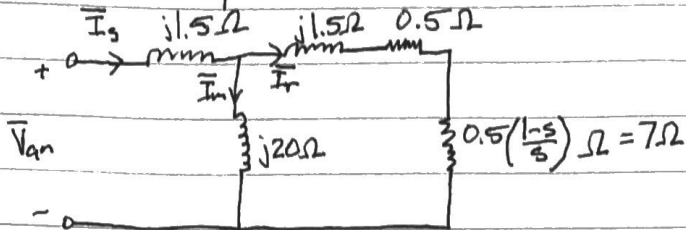
c) 187.0 Nm

d) 89.3 Nm

# Fall 2003 Final

7) 3  $\phi$ , 6-pole, 60 Hz, 440 V

$$\omega_m = 1120 \text{ rpm}$$



$$a) s = \frac{\omega_s - \left(\frac{P}{2}\right)\omega_m}{\omega_s} = \frac{3600 - \left(\frac{6}{2}\right)(1120)}{3600} \Rightarrow s = 0.0667$$

$$f_r = s f_s \Rightarrow f_r = 0.0667(60) \Rightarrow \boxed{f_r = 4 \text{ Hz}}$$

$$b) \bar{Z}_{eq} = j1.5 + \left( \frac{1}{7.5 + j1.5} + \frac{1}{j20} \right)^{-1} \Rightarrow \bar{Z}_{eq} = 5.786 + j4.914 \Omega$$

$$= 7.591 \angle 40.34^\circ \Omega$$

$$\bar{I}_s = \frac{\bar{V}_{an}}{\bar{Z}_{eq}} \Rightarrow \bar{I}_s = \frac{440 \angle 0^\circ}{7.591 \angle 40.34^\circ} \Rightarrow \boxed{\bar{I}_s = 33.465 \angle -40.34^\circ \text{ A}}$$

$$c) \bar{I}_s = \bar{I}_r + \bar{I}_L$$

$$\bar{I}_r = \frac{\bar{V}_{an} - j1.5 \bar{I}_s}{7.5 + j1.5} \Rightarrow \bar{I}_r = \frac{440 \angle 0^\circ - 50.193 \angle 49.16^\circ}{7.5 + j1.5} \Rightarrow \bar{I}_r = \frac{221.540 - j39.262}{7.5 + j1.5}$$

$$\bar{I}_r = 27.421 - j10.586 \Rightarrow \bar{I}_r = 29.393 \angle -21.11^\circ$$

$$P_{AG} = 3 |\bar{I}_r|^2 \left( \frac{R_r}{s} \right) \Rightarrow P_{AG} = 3 (29.393)^2 (7.5) \Rightarrow P_{AG} = 19,438.84 \text{ W}$$

$$T^c = \frac{P_{AG}}{\left(\frac{P}{2}\right)\omega_s} \Rightarrow \boxed{T^c = 154.69 \text{ Nm}}$$

$$d) \text{ at start, } s=1, \bar{Z}_{eq} = j1.5 + \left( \frac{1}{0.5j1.5} + \frac{1}{j20} \right)^{-1} \Rightarrow \bar{Z}_{eq} = 2.937 \angle 81.54^\circ$$

$$\bar{I}_s = \frac{\bar{V}_{an}}{\bar{Z}_{eq}} \Rightarrow \boxed{\bar{I}_s = 86.49 \angle -81.54^\circ \text{ A}}$$